



# St Bartholomew's CE Primary School Calculation Policy

## Year 1-6

This policy follows a Concrete, Pictorial and Abstract approach to Mastery Maths teaching.

Some images have been taken from NCETM PD Materials.

This is a working document and subject to change.



St Bartholomew's CE Primary School Calculation Policy

Adding 1 and 2

Bonds to 10

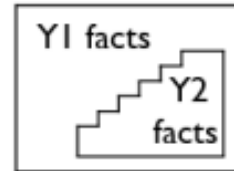
Adding 10

Bridging/  
compensating

Doubles

Adding 0


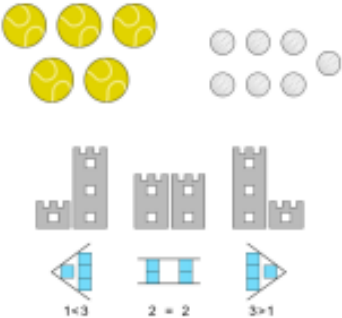
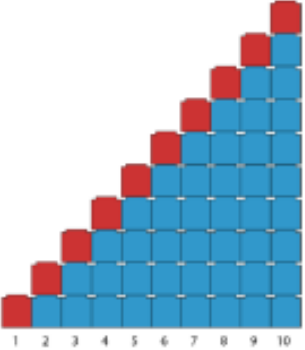
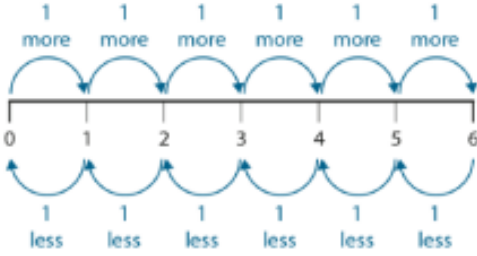
Near doubles



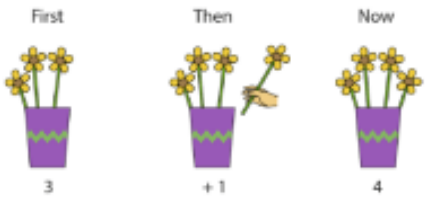
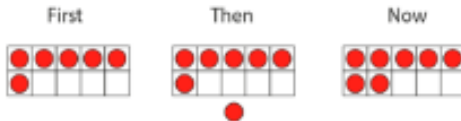
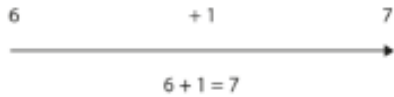

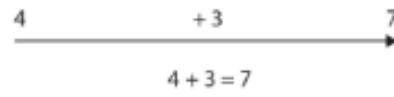
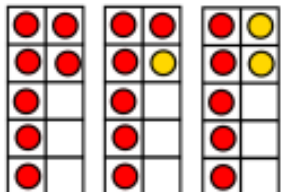
Y1/2

+	0	1	2	3	4	5	6	7	8	9	10
0	0+0	0+1	0+2	0+3	0+4	0+5	0+6	0+7	0+8	0+9	0+10
1	1+0	1+1	1+2	1+3	1+4	1+5	1+6	1+7	1+8	1+9	1+10
2	2+0	2+1	2+2	2+3	2+4	2+5	2+6	2+7	2+8	2+9	2+10
3	3+0	3+1	3+2	3+3	3+4	3+5	3+6	3+7	3+8	3+9	3+10
4	4+0	4+1	4+2	4+3	4+4	4+5	4+6	4+7	4+8	4+9	4+10
5	5+0	5+1	5+2	5+3	5+4	5+5	5+6	5+7	5+8	5+9	5+10
6	6+0	6+1	6+2	6+3	6+4	6+5	6+6	6+7	6+8	6+9	6+10
7	7+0	7+1	7+2	7+3	7+4	7+5	7+6	7+7	7+8	7+9	7+10
8	8+0	8+1	8+2	8+3	8+4	8+5	8+6	8+7	8+8	8+9	8+10
9	9+0	9+1	9+2	9+3	9+4	9+5	9+6	9+7	9+8	9+9	9+10
10	10+0	10+1	10+2	10+3	10+4	10+5	10+6	10+7	10+8	10+9	10+10

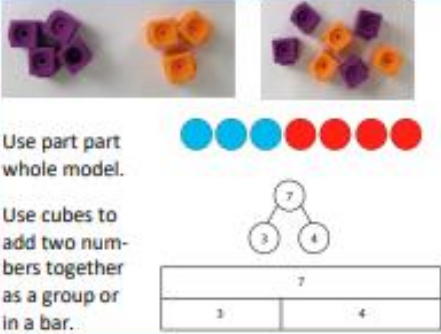
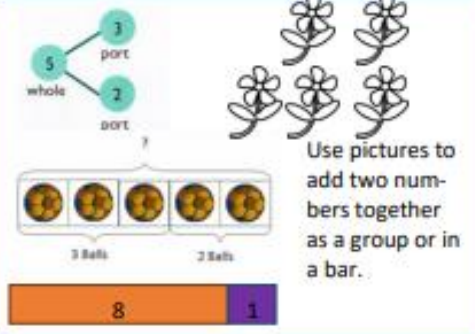
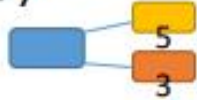
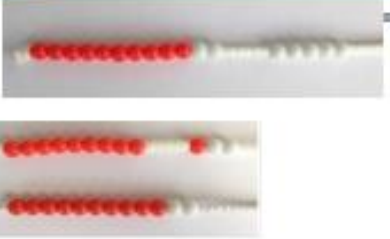
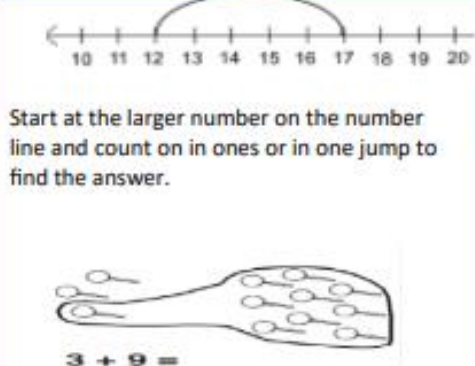
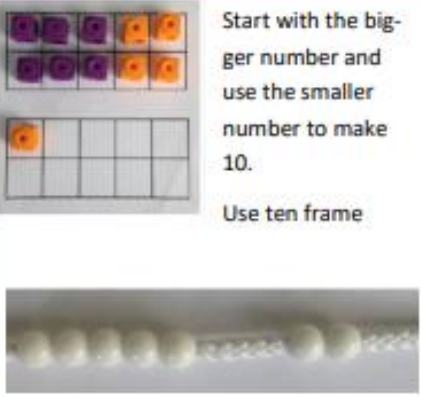
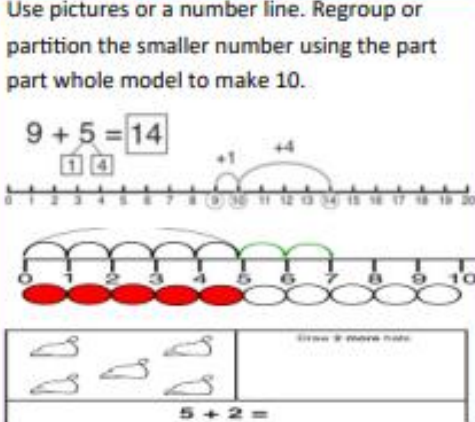
**SUBTRACTION -**  
**ADDITION +**

Objective, Strategy & Key Vocabulary	Concrete	Pictorial	Abstract
Comparing Objects, groups of objects  <b>Length, weight, mass, heavier, lighter, same, equal</b>	People's height, distance, mass. Use of pan balances using numicon to show equivalence, < >  Comparing multiple objects  Use of concrete materials eg. Compare bears, jewels, cubes etc to create groups of different sizes to compare		
Using < > and =  <b>Fewer, more, less than, more than, equal to, fewer than</b>	Use a multilink staircase in two colours		Use variation with missing boxes and missing symbols.  $3 \bigcirc 4$ $4 > \square$  $2 \bigcirc 2$ $\square < 6$
Finding one more, finding one less			One more/less sentences – example one: 1 more than 3 is <input type="text"/> 1 less than 2 is <input type="text"/>  1 more than <input type="text"/> is 1 1 less than <input type="text"/> is 1

# Y1 ADDITION +


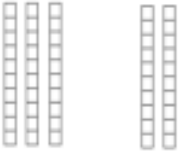
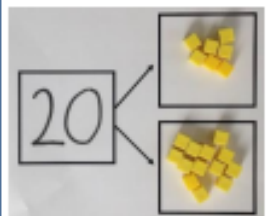
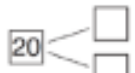
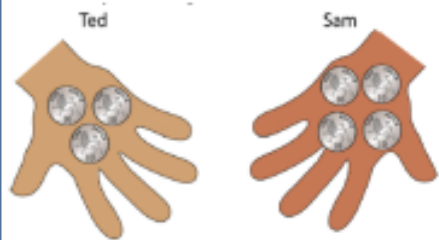
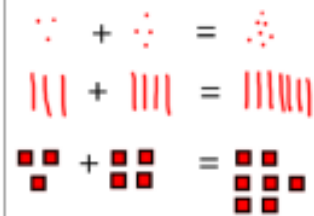



Objective, Strategy & Key Vocabulary	Concrete	Pictorial	Abstract
<p>Adding 1 gives 1 more</p>	<p>First      Then      Now</p>  <p>3      +1      4</p>	<p>First      Then      Now</p> 	
<p>Augmentation— increasing an amount</p>	<p>Use FIRST, THEN, NOW and range of practical situations for showing augmentation.</p> <p>E.g. first there were three chn on carpet then 2 more came. Now there are 5 chn on the carpet.</p>	<p>First      Then      Now</p> 	
<p>Stories of numbers within 10</p>	<p>Children should work with doubled sided counters and ten frame.</p> <p>Start with 7 red, turn one over, tell me the 'story'?</p> <p>Turn one more over. What is the 'story'?</p> <p>Continue.</p> <p>Complete this for stories of all numbers up to 10.</p>	 <p>7 + 0 = 7 6 + 1 = 7 5 + 2 = 7 etc</p> <p>Complete for all numbers up to 10</p>	<p>7 + 0 = 7</p> <p>6 + 1 = 7</p> <p>5 + 2 = 7</p> <p>4 + 3 = 7</p> <p>3 + 4 = 7</p> <p>2 + 5 = 7</p> <p>1 + 6 = 7</p> <p>0 + 7 = 7</p>

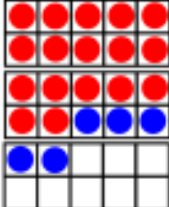
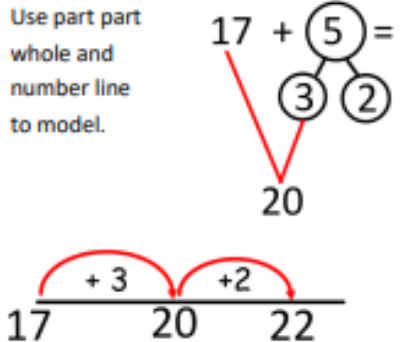

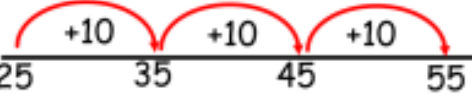
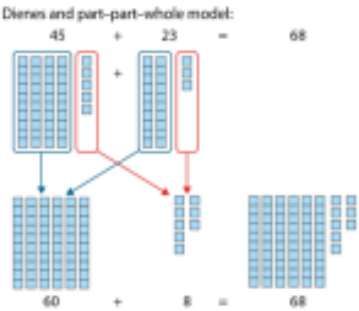
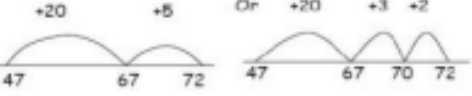
# Y1 ADDITION +

Objective & Strategy & Key Vocabulary	Concrete	Pictorial	Abstract
Combining two parts to make a whole: part- whole model	 <p>Use part part whole model.</p> <p>Use cubes to add two numbers together as a group or in a bar.</p>	 <p>Use pictures to add two numbers together as a group or in a bar.</p>	$4 + 3 = 7$  $10 = 6 + 4$ <p>Use the part-part whole diagram as shown above to move into the abstract.</p>
Regrouping to make 10.  <i>This is an essential skill for column addition later.</i>	 <p><math>5 + 2 = 7</math></p> <p>2 more than 5.</p>	 <p>Start at the larger number on the number line and count on in ones or in one jump to find the answer.</p> <p><math>3 + 9 =</math></p>	$7 + 4 = 11$ <p>If I am at seven, how many more do I need to make 10. How many more do I add on now?</p>
Represent & use number bonds and related subtraction facts within 20	 <p>Start with the bigger number and use the smaller number to make 10.</p> <p>Use ten frame</p>	<p>Use pictures or a number line. Regroup or partition the smaller number using the part part whole model to make 10.</p> <p><math>9 + 5 = 14</math></p>  <p><math>5 + 2 =</math></p>	<p>Emphasis should be on the language</p> <p>'1 more than 5 is equal to 6.'</p> <p>'2 more than 5 is 7.'</p> <p>'8 is 3 more than 5.'</p>

# Y1 ADDITION +

# Y2 ADDITION +

Objective & Strategy & Key Vocabulary	Concrete	Pictorial	Abstract
Adding multiples of ten	$50 = 30 + 20$  Model using dienes and bead strings	 __ tens and __ tens makes __ tens Use representations for base ten.	$20 + 30 = 50$ $70 = 50 + 20$ $40 + \square = 60$ $\square + 30 = 50$
Use known number facts <b>Part part whole</b>	 Children explore ways of making numbers within 20	 $\square + \square = 20$ $20 - \square = \square$ $\square + \square = 20$ $20 - \square = \square$	$\square + 1 = 16$ $16 - 1 = \square$ $1 + \square = 16$ $16 - \square = 1$
Using known facts		 Children draw representations of H,T and O	$3 + 4 = 7$ Leads to $30 + 40 = 70$ Leads to $300 + 400 + 700$ <i>'3 things and 4 things is always 7 things'</i>
Bar model	 $3 + 4 = 7$	 $3 + 5 = 8$	 $14 + 16 = 30$

Objective & Strategy & Key Vocabulary	Concrete	Pictorial	Abstract				
Add a two digit number and ones	 <p><math>17 + 5 = 22</math></p> <p>Use ten frame to make 'magic ten'</p> <p>Children explore the pattern.</p> <p><math>17 + 5 = 22</math></p> <p><math>27 + 5 = 32</math></p>	<p>Use part part whole and number line to model.</p> <p><math>17 + 5 = 22</math></p> 	<p><math>17 + 5 = 22</math></p> <table border="1" data-bbox="1612 319 1848 406"> <tr><td colspan="2">22</td></tr> <tr><td>17</td><td>5</td></tr> </table> <p>Explore related facts</p> <p><math>17 + 5 = 22</math>      <math>22 = 17 + 5</math></p> <p><math>5 + 17 = 22</math>      <math>22 = 5 + 17</math></p> <p><math>22 - 17 = 5</math>      <math>17 = 22 - 5</math></p> <p><math>22 - 5 = 17</math>      <math>5 = 22 - 17</math></p>	22		17	5
22							
17	5						
Add a 2 digit number and tens	 <p><math>25 + 10 = 35</math></p> <p>Explore that the ones digit does not change</p>	<p><math>25 + 30 = 55</math></p> 	<p><math>27 + 10 = 37</math></p> <p><math>27 + 20 = 47</math></p> <p><math>27 + \square = 57</math></p> <p><math>\square + 30 = 67</math></p>				
Add two 2-digit numbers without bridging. 'Friendly numbers'	<p>Model using dienes, place value counters and numicon</p> <p>Dienes and part-part-whole model:</p> <p><math>45 + 23 = 68</math></p>  <p><math>60 + 8 = 68</math></p>	 <p>Use number line and bridge ten using part whole if necessary.</p>	<p><math>25 + 47</math></p> <p><math>20 + 5</math>      <math>40 + 7</math></p> <p><math>20 + 40 = 60</math></p> <p><math>5 + 7 = 12</math></p> <p><math>60 + 12 = 72</math></p>				

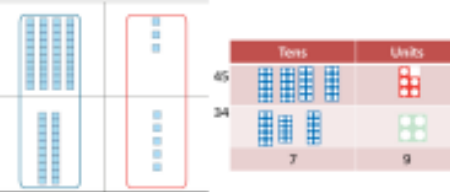

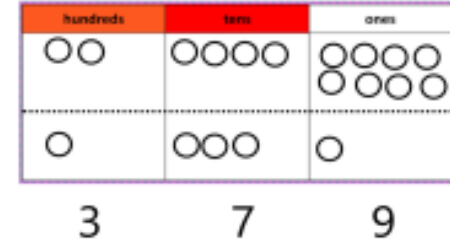

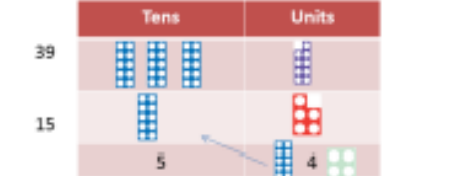
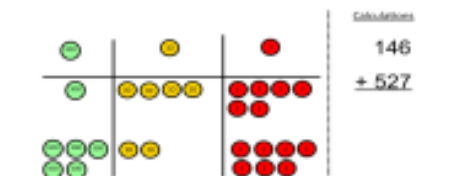
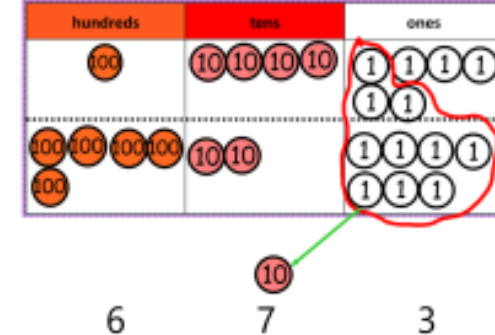
# Y2 ADDITION +

# Y2 ADDITION +

Objective & Strategy & Key Vocabulary	Concrete	Pictorial	Abstract
Add any two 2-digit numbers	<p>Dienes and part-part-whole model</p> $26 + 37 = 63$	$26 + 30 + 7$	$24 + 38 = \square$ $29 + \square = 51$ $38 + 24 = \square$ $\square + 22 = 51$
Add three 1-digit numbers	<p>Combine to make magic 10 first where relevant, or bridge 10 then add third</p>	<p>Use language of first, then, then, now</p> <p>Pictorial:</p> <p>First      Then      Then      Now</p> <p>Use part part whole to show magic ten</p> $2 + 3 + 8$ $10 + 3 = 13$	$\textcircled{4} + 7 + \textcircled{6} = \boxed{10} + \boxed{7}$ $= \boxed{17}$ <p>Combine the two numbers that make/bridge ten then add on the third.</p>
Adding two numbers that bridge 10.	<p>Use double sided counters and ten frames. Move counters to fill the ten frame and make Magic 10</p>	<p>Show on a number line how 5 is portioned into adding three, then adding 2.</p>	$7 + 5$

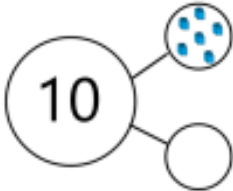
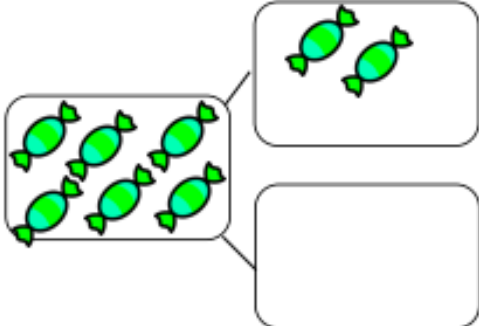
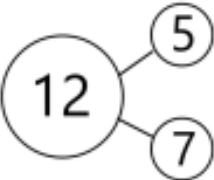
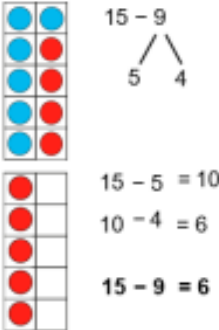
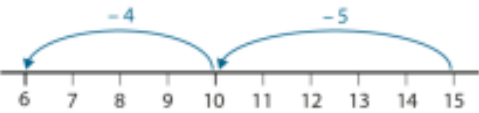
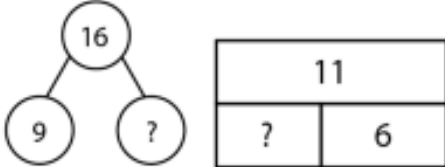
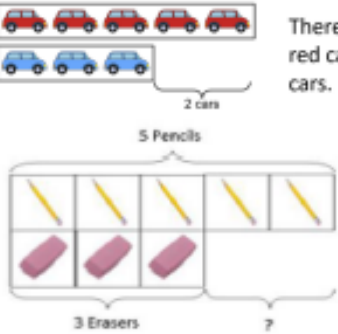
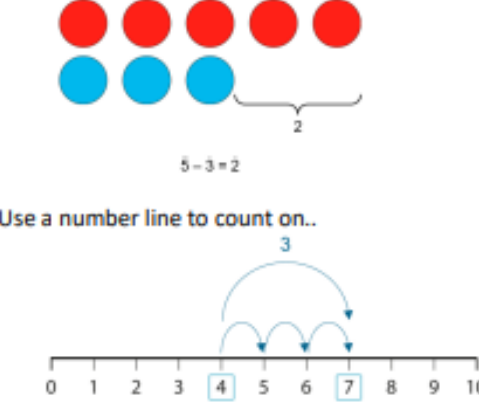


# Y3 ADDITION +

<b>Objective &amp; Strategy</b> <i>Key Vocab</i>	<b>Concrete</b> When moving from concrete to pictorial, show concrete alongside pictorial. Show pictorial alongside abstract when moving to abstract.	<b>Pictorial</b>	<b>Abstract</b>
<p>Column Addition—no re-grouping (friendly numbers)</p> <p>Add two or three 2 or 3-digit numbers.</p>	<p>Model using Dienes or numicon</p>  <p>Add together the ones first, then the tens.</p>  <p>Move to using place value counters</p>	<p>Children move to drawing the counters using a tens and one frame.</p>  <p>3      7      9</p> <p>tens      ones</p> 	$\begin{array}{r} 248 \\ + 131 \\ \hline 379 \end{array}$ <p>Add the ones first, then the tens, then the hundreds.</p>
<p>Column Addition with re-grouping.</p> <p>Use language of 'take and make' to describe carrying</p>	 <p>Exchange ten ones for a ten. Model using numicon and pv counters.</p>  <p>Calculations</p> $\begin{array}{r} 146 \\ + 527 \\ \hline \end{array}$	<p>Children can draw a representation of the grid to further support their understanding, carrying the ten <u>underneath</u> the line.</p>  <p>6      7      3</p>	<p>Use expanded method ONLY WHEN NEEDED</p> $\begin{array}{r} 20 + 5 \\ 40 + 8 \\ 60 + 13 = 73 \end{array}$ <p>Start by partitioning the numbers before formal column to show the exchange.</p> $\begin{array}{r} 536 \\ + 85 \\ \hline 621 \\ 11 \end{array}$

Objective & Strategy & Key Vocabulary	Concrete	Pictorial	Abstract
<p>Y4—add numbers with up to 4 digits</p>	<p>Children continue to use dienes or pv counters to add, exchanging ten ones for a ten and ten tens for a hundred and ten hundreds for a thousand.</p>	<p>Draw representations using pv grid.</p>	$\begin{array}{r} 2634 \\ + 4517 \\ \hline 7141 \\ \hline 1 \quad 1 \end{array}$ <p>Continue from previous work to carry ones, tens and hundreds.</p> <p>Relate to money and measures.</p>
<p>Y5—add numbers with more than 4 digits.</p> <p>Add decimals with 2 decimal places, including money.</p>	<p>As year 4</p> <p>Introduce decimal place value counters</p>	$2.37 + 81.79$	$\begin{array}{r} 22,634 \\ + 15,673 \\ \hline 38,307 \\ \hline 1 \quad 1 \end{array}$ $\begin{array}{r} \text{£ } 127.67 \\ + \text{£ } 38.45 \\ \hline \text{£ } 166.12 \\ \hline 1 \quad 1 \quad 1 \end{array}$
<p>Y6—add several numbers of increasing complexity</p> <p>Including adding money, measure and decimals with different numbers of decimal points.</p>	<p>Some children may need to use manipulatives and/or representations for longer. See year 5</p>		$\begin{array}{r} 89,472 \\ 63,673 \\ + 3,016 \\ \hline 156,161 \\ \hline 1 \quad 1 \quad 1 \quad 1 \end{array}$ $\begin{array}{r} 1.437 \\ 0.600 \\ + 3.020 \\ \hline 4.057 \\ \hline 1 \end{array}$ <p>Insert zeros for place holders.</p>

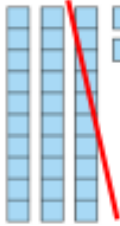

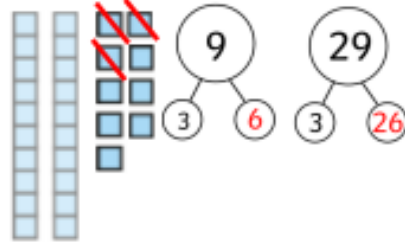
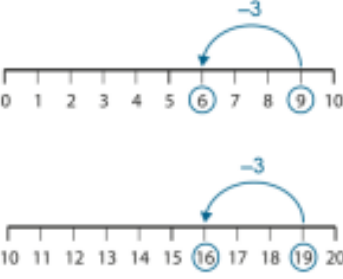
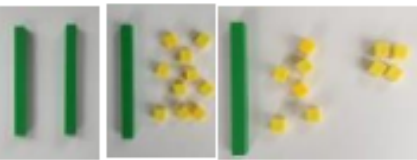
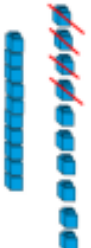

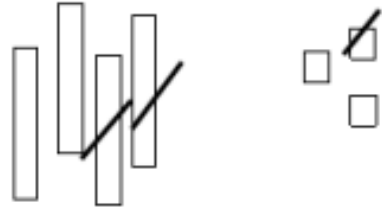
# Y4-6 ADDITION +

Objective & Strategy	Concrete	Pictorial	Abstract
<p>Represent and use number bonds and related subtraction facts within 20</p> <p>Part-Part-Whole model</p>	 <p>Link to addition. Use PPW model to model the inverse.</p> <p>If 10 is the whole and 6 is one of the parts, what's the other part?</p> <p><math>10 - 6 = 4</math></p>	 <p>Use pictorial representations to show the part.</p>	<p>Move to using numbers within the part whole model.</p>  <p><math>12 - 5 = 7</math>  <math>12 - 7 = 5</math>  <math>7 = 12 - 5</math>  <math>5 = 12 - 7</math></p>
<p>Subtract by making ten</p>	<p><math>15 - 9</math></p> <p>Make 15 on the ten frame. Take 5 away to make ten, then take 4 more away so that you have taken 9.</p>  <p><math>15 - 5 = 10</math>  <math>10 - 4 = 6</math>  <math>15 - 9 = 6</math></p>	<p><math>15 - 9</math></p>  <p>Jump back 5 first, then another 4. Use ten as the stopping point.</p>	<p><math>16 - 9</math></p> <p>How many do we take off first to get to 10? How many left to take off?</p> 
<p>Compare numbers by finding the difference.</p>	 <p>There are 2 more red cars than blue cars.</p> <p>There are 2 more pencils than erasers.</p>	 <p>Use a number line to count on..</p>	<p>Hannah has 12 sweets and her sister has 5. How many more does Hannah have than her sister?</p>

# Y1 SUBTRACTION -


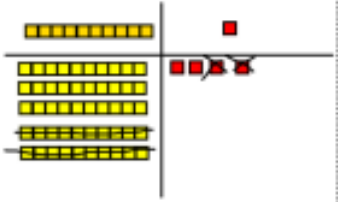
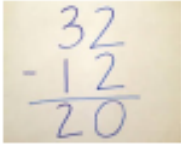
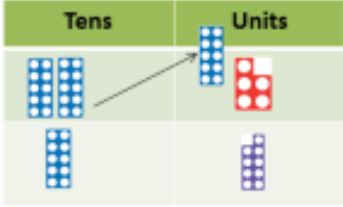
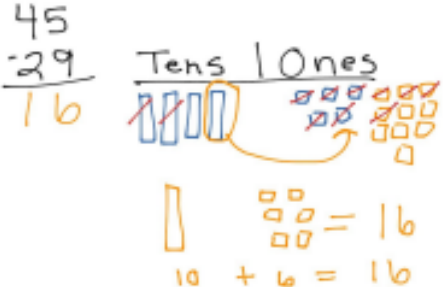
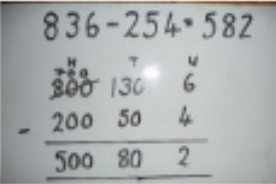
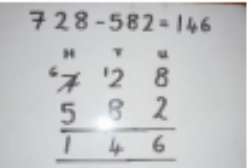
Objective & Strategy	Concrete	Pictorial	Abstract
<p>Subtracting by making 10</p>	<p>Make 15 on the ten frame. Take 5 away to make ten, then take 4 more away so that you have taken 9.</p>	<p><math>15 - 9 =</math></p> <p>Jump back 5 first, then another 4. Use ten as the stopping point.</p>	<p><math>16 - 9 =</math></p> <p>How many do we take off first to get to 10? How many left to take off?</p>
<p>Counting on to next ten</p> <p><i>Progression should be crossing one ten, crossing more than one ten, crossing the hundreds.</i></p>	<p><math>34 - 28 =</math></p> <p><math>34 - 28</math></p> <p>Use a bead bar or bead strings to model counting to next ten and the rest.</p> <p>28 to 30 is 2, 30 to 34 is 4. So, <math>34 - 28 = 6</math></p>	<p>Use a number line to count on to next ten and then the rest.</p> <p>Begin with bead line, move to landmarked line then to ENL.</p>	<p><math>93 - 76 = 17</math></p> <p><math>76 \rightarrow 80 = 4</math></p> <p><math>80 \rightarrow 93 = 13</math></p> <p><math>13 + 4 = 17</math></p>
<p>Subtractions as difference</p>	<p>Ben is ten years old Charlotte is three years old</p> <p>10 years old</p> <p>3 years old</p> <p>difference of 7 years</p>	<p>7</p> <p>4</p> <p>3</p> <p>3</p> <p>0 1 2 3 4 5 6 7 8 9 10</p>	<p>The difference between 24 and 16 is 8.</p>

# Y2 SUBTRACTION -

Objective & Strategy	Concrete	Pictorial	Abstract
Subtracting a multiple of 10	 <p><math>32 - 10 = 22</math></p> <p>Children use dienes, PV counters or Numicon.</p> <p>They remove the correct number of tens</p>	 <p>Children draw rods and cubes and cross off multiples of ten.</p>	$64 - 10 = \square$ $64 - 20 = \square$ $64 - 30 = \square$ $64 - \square = 24$ $\square - 50 = 14$
Subtract a single digit from a two digit number  No regrouping	 <p>Explore that <math>9 - 3 = 6</math> so <math>29 - 3 = 26</math> etc</p>	 <p><math>9 - 3 = 6</math></p> <p><math>19 - 3 = 16</math></p>	$9 - 3 = 6$ $19 - 6 = 13$ $29 - 6 = 23$ etc
Regroup a ten into ten ones	 <p>Use a PV chart to show how to change a ten into ten ones, use the term 'take and make'.</p>	$20 - 4 = 16$ 	$20 - 4 = 16$
Partitioning to subtract without regrouping.  'Friendly numbers'	$34 - 13 = 21$  <p>Use Dienes to show how to partition the number when subtracting without regrouping.</p>	$43 - 21 = 22$ <p>Children draw representations of Dienes and cross off.</p> 	$43 - 21 = 22$

# Y2 SUBTRACTION -

# Y3 SUBTRACTION -

Objective & Strategy	Concrete	Pictorial	Abstract
<p>Column subtraction without regrouping (friendly numbers)</p>	 <p>47 - 32</p> <p>Use base 10 or Numicon to model</p>	 <p>Calculations</p> $\begin{array}{r} 54 \\ - 22 \\ \hline 32 \end{array}$ <p>Draw representations to support understanding</p>	<p>Intermediate step may be needed to lead to clear subtraction understanding.</p> $47 - 24 = 23$ $\begin{array}{r} 40 + 7 \\ - 20 + 4 \\ \hline 20 + 3 \end{array}$ <p>Leading to compact method.</p> 
<p>Column subtraction with regrouping</p>	 <p>Begin with base 10 or Numicon. Move to pv counters, modelling the exchange of a ten into ten ones. Use the phrase 'take and make' for exchange.</p>	 $\begin{array}{r} 45 \\ - 29 \\ \hline 16 \end{array}$ <p>Children may draw base ten or PV counters and cross off.</p>	<p>Begin by partitioning into pv columns</p>  $\begin{array}{r} 836 - 254 = 582 \\ \begin{array}{r} \text{h} \quad \text{t} \quad \text{u} \\ 800 \quad 30 \quad 6 \\ - 200 \quad 50 \quad 4 \\ \hline 500 \quad 80 \quad 2 \end{array} \end{array}$ <p>Then move to formal method.</p>  $\begin{array}{r} 836 - 254 = 582 \\ \begin{array}{r} \text{h} \quad \text{t} \quad \text{u} \\ 836 \\ - 254 \\ \hline 582 \end{array} \end{array}$

Objective & Strategy	Concrete	Pictorial	Abstract
<p>Subtracting tens and ones</p> <p>Year 4 subtract with up to 4 digits.</p> <p><i>Introduce decimal subtraction through context of money</i></p>	<p>234 - 179</p> <p>Model process of exchange using Numicon, base ten and then move to PV counters.</p>	<p>Children to draw pv counters and show their exchange—see Y3</p>	<p>Use the phrase 'take and make' for exchange</p>
<p>Year 5- Subtract with at least 4 digits, including money and measures.</p> <p><i>Subtract with decimal values, including mixtures of integers and decimals and aligning the decimal point.</i></p>	<p>As Year 4</p>	<p>Children to draw pv counters and show their exchange—see Y3</p>	<p>Use zeros for place-holders.</p>
<p>Year 6—Subtract with increasingly large and more complex numbers and decimal values.</p>			

Y4-6


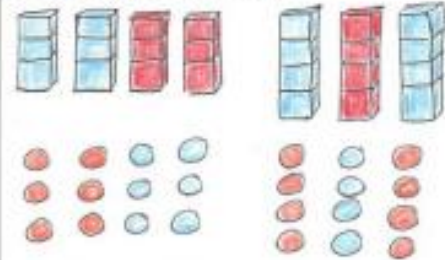
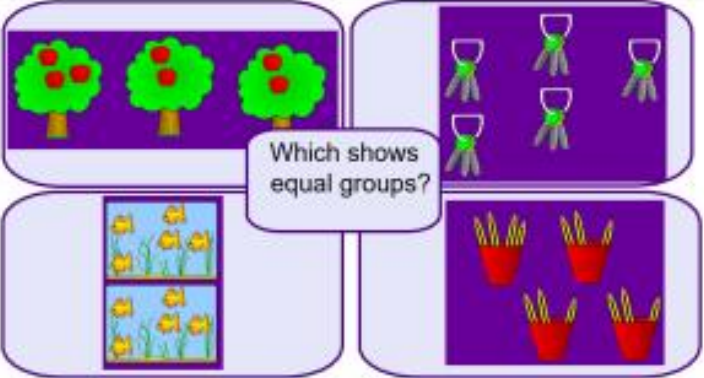
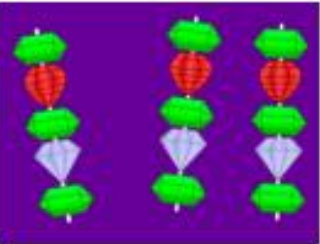
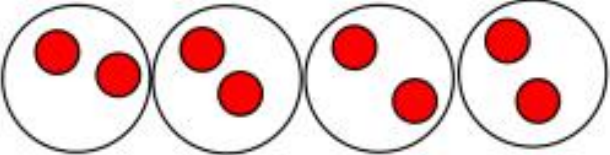
# SUBTRACTION -

# Y1 MULTIPLICATION X

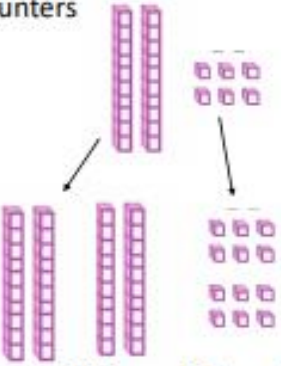
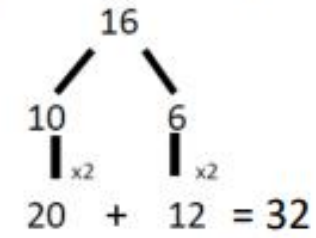

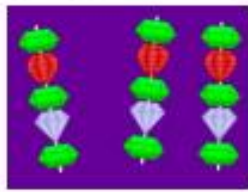



Objective & Strategy	Concrete	Pictorial
<p>Double numbers to 10</p>	<p>Use practical activities using manipulatives including cubes and Numicon to demonstrate doubling</p>	<p>Draw pictures and bar models to show how to double numbers</p> <p>Double 4 is 8</p>
<p>Counting in groups of 2</p>	<p>Count in 2s using real life objects and contexts.</p>	<p>Children make representations to show counting in multiples of 2. Count in multiples of a number aloud.</p> <p>⋮ Show jumps of 2 on a number line</p>
<p>Counting in groups of 10</p>	<p>Use real life objects and contexts to count in groups of 10</p>	<p>Use and draw representations for counting in multiples of 10. Count in multiples of 10 aloud</p> <p>Show jumps of 10 on a number line</p>
<p>Counting in groups of 5</p>	<p>Use real life objects and contexts to count in groups of 5</p>	<p>Use and draw representations for counting in multiples of 5. Count in 5s aloud.</p>




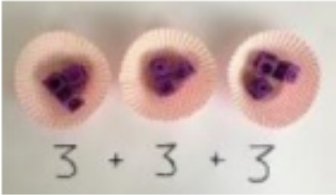
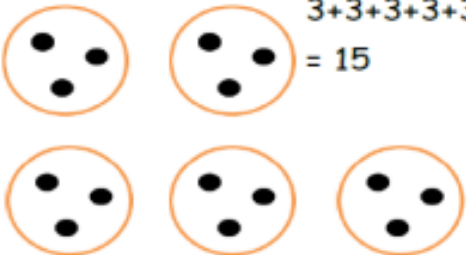

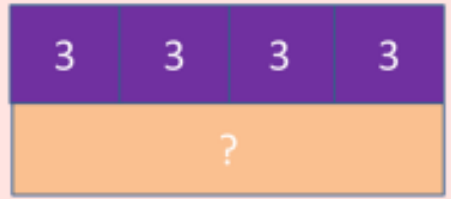



# Y1 MULTIPLICATION X

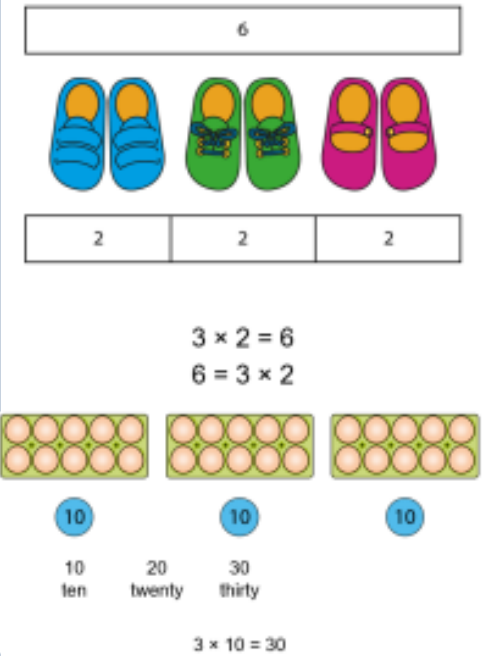
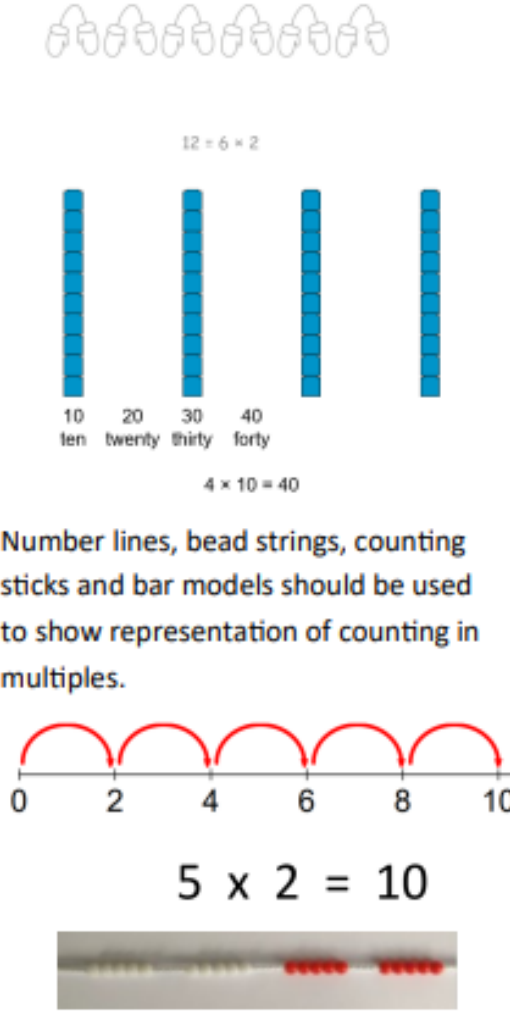
Objective & Strategy	Concrete	Pictorial
Understand and use arrays	<p>Use objects laid out in arrays to find the answers to 2 lots of 5, 3 lots of 2 etc.</p> 	<p>Make and draw representations of arrays to show understanding</p> 
Equal/non equal groups	<p>Use real life objects and contexts to examine equal and non-equal groups.</p>  <p>Which shows equal groups?</p>  <p>There are 3 equal groups. There are 5 in each group.</p>	<p>Children make/match representations of real life problems to show equal groups and find the total.</p>  <p>There are 4 equal groups. There are 2 in each group. There are 8 altogether.</p>

# Y2 MULTIPLICATION X

Objective & Strategy	Concrete	Pictorial	Abstract
<p>Double a 2-digit number</p>	<p>Model doubling using dienes and PV counters</p>  <p><math>40 + 12 = 52</math></p>	<p>Draw pictures and representations to show how to double numbers</p>	<p>Partition a number and then double each part before recombining it back together</p>  <p><math>20 + 12 = 32</math></p>
<p>Understand equal and non-equal groups</p>	<p>These are non-equal groups</p>  <p>These are equal groups</p>   <p>There are 5 equal groups. Each group has 3 cakes.</p>	<p>Make representations and drawings of equal groups</p>   <p>I have 4 groups of 3.</p>	





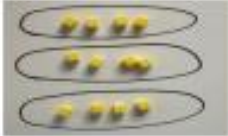
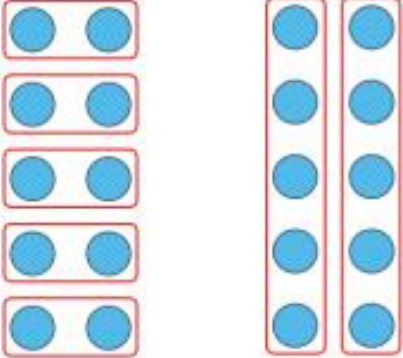
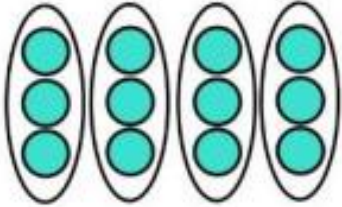
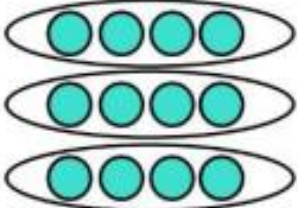

# Y2 MULTIPLICATION X

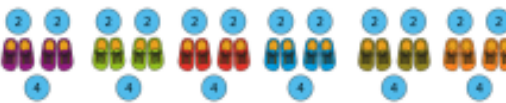

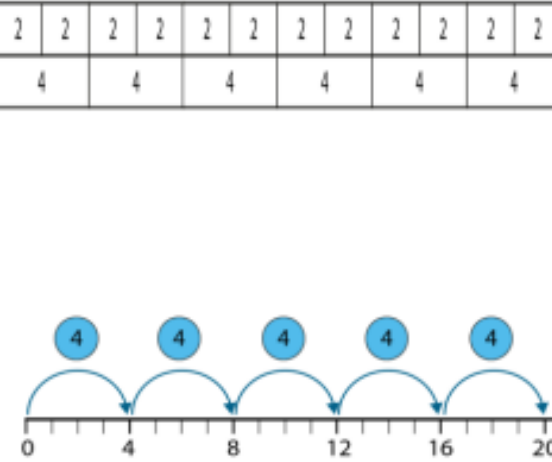
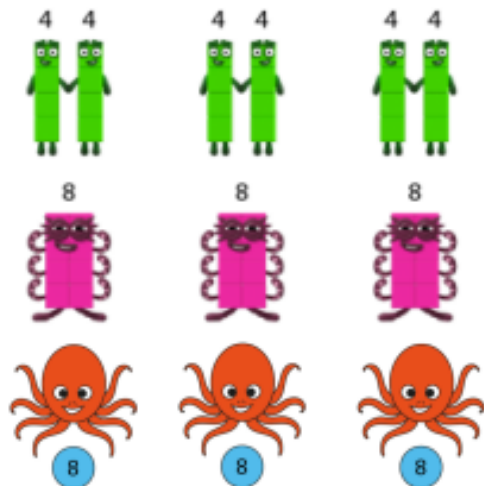
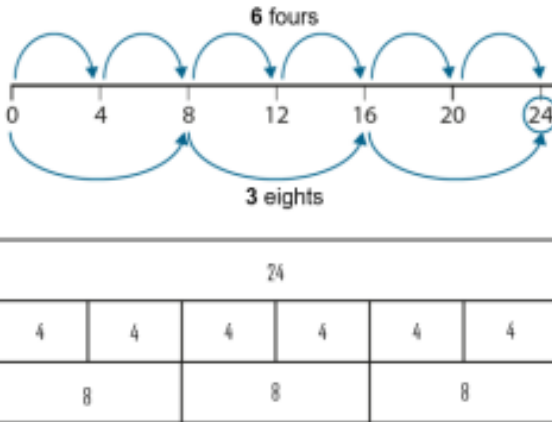
Objective & Strategy	Concrete	Pictorial	Abstract
<p>Use repeated addition for multiplications</p>	<p>Use objects and real life contexts.</p>  $2 + 2 + 2 + 2 + 2 = 10$ <p>There are 5 groups of 2. There are 10 socks altogether.</p>  $3 + 3 + 3$ <p>There are 3 groups of 3. There are 9 altogether.</p>	<p>Make and draw representations to show repeated addition</p> <p>There are 3 sweets in one bag. How many sweets are in 5 bags altogether?</p>  $3 + 3 + 3 + 3 + 3 = 15$ <p>Use bar models for representations of repeated additions.</p> 	<p>Create number sentences using repeated addition to match representations.</p>  $3 + 3 + 3 + 3 = 12$
<p>Relate repeated addition to multiplication using the x sign.</p>	<p>Write multiplication sentences to match repeated addition.</p>  $2 + 2 + 2 + 2$ $4 \times 2$	<p>Children make and draw representations and record both an addition sentence and a multiplication sentence.</p>  $1 + 1 + 1 + 1 + 1 + 1 = 6$ $6 \times 1 = 6$  $\square \times \square = 6$	<p>Write multiplication sentences to match repeated addition, without the support of representations.</p> $2 + 2 + 2 + 2 + 2 = 10$ $5 \times 2 = 10$

Objective & Strategy	Concrete	Pictorial	Abstract																				
<p>Understand the 2, 5 and 10 times table</p>	<p>Use objects and real life contexts for multiples of 2, 5 and 10</p>  <p><math>3 \times 2 = 6</math> <math>6 = 3 \times 2</math></p> <p><math>3 \times 10 = 30</math></p>	<p>Make and draw representations for 2, 5 and 10 times tables</p>  <p><math>12 = 6 \times 2</math></p> <p><math>4 \times 10 = 40</math></p> <p><math>5 \times 2 = 10</math></p>	<p>Understand the terms factor and product</p> <table border="1" data-bbox="1429 379 1910 459"> <tr> <td>3</td> <td>×</td> <td>2</td> <td>=</td> <td>6</td> </tr> <tr> <td>factor</td> <td>×</td> <td>factor</td> <td>=</td> <td>product</td> </tr> </table> <table border="1" data-bbox="1429 518 1910 598"> <tr> <td>6</td> <td>=</td> <td>3</td> <td>×</td> <td>2</td> </tr> <tr> <td>product</td> <td>=</td> <td>factor</td> <td>×</td> <td>factor</td> </tr> </table> <p>Count in multiples of a number aloud.</p>	3	×	2	=	6	factor	×	factor	=	product	6	=	3	×	2	product	=	factor	×	factor
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# Y2 MULTIPLICATION X

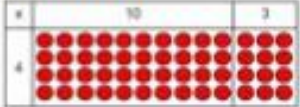
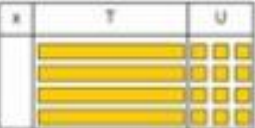
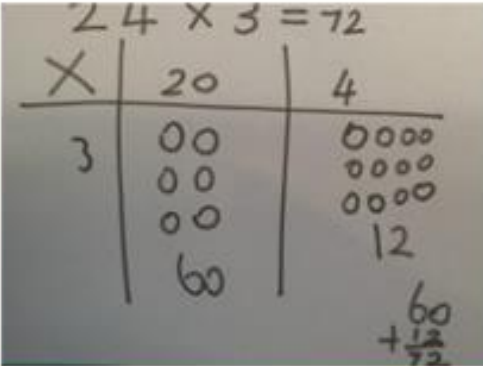
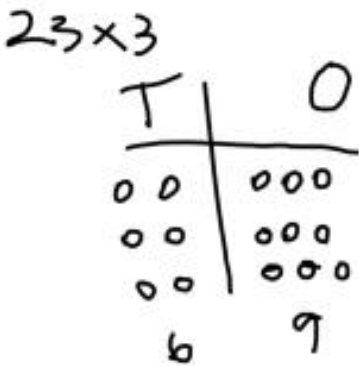
# Y2 MULTIPLICATION X

Objective & Strategy	Concrete	Pictorial	Abstract
<p>Multiplication is commutative</p>	<p>Create arrays using counters and cubes and Numicon.</p>    <p>Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.</p>  	<p>Use representations of arrays to show different calculations and explore commutativity.</p>  <p> <math>5 \times 2 = 10</math>      <math>5 \times 2 = 10</math>                      5 groups of 2    2 groups of 5                      2, five times    5, two times                 </p>  	<p> <math>12 = 3 \times 4</math>  <math>12 = 4 \times 3</math> </p> <hr/> <p>Use an array to write multiplication sentences and reinforce repeated addition.</p>  <p> <math>5 + 5 + 5 = 15</math>  <math>3 + 3 + 3 + 3 + 3 = 15</math>  <math>5 \times 3 = 15</math>  <math>3 \times 5 = 15</math> </p>

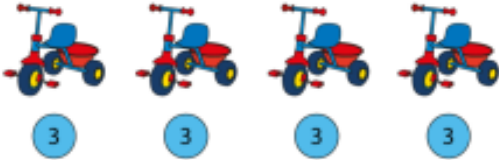
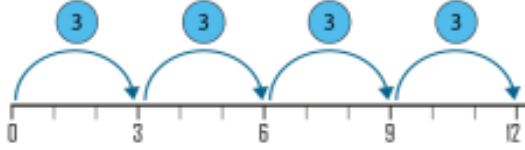
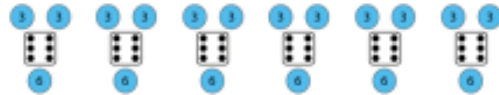


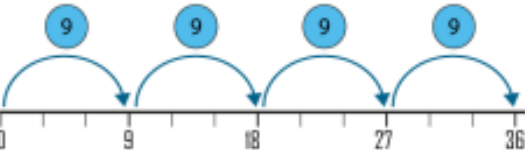
Objective & Strategy	Concrete	Pictorial	Abstract
<p><i>Understand the 4 times table</i></p>	<p>We can double our 2 times table to get the 4 times table</p>  <p>Pupils revise 2 times table from year 2 and make link that this can be doubled to obtain 4 times table.</p> <p>How many wheels? Count in groups of 4.</p> 		<p><math>12 \times 2 = 24</math></p> <p><math>6 \times 2 = 24</math></p> <p>There are 20 wheels.</p> <p><math>5 \times 4 = 20</math></p> <p><math>4 \times 5 = 20</math></p>
<p><i>Understand the 8 times table</i></p>	<p>We can double our 4 times table to get the 8 times table</p> 		<p><math>6 \times 4 = 24</math></p> <p><math>3 \times 8 = 24</math></p>

# Y3 MULTIPLICATION X


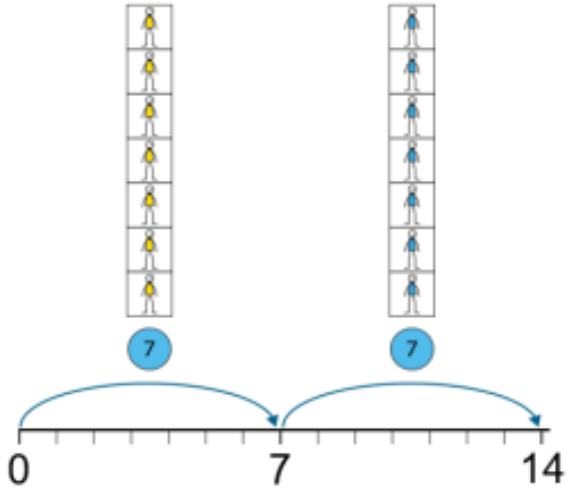
# Y3 MULTIPLICATION X

Objective & Strategy	Concrete	Pictorial	Abstract								
<p>Multiplying 2-digit by 1 digit using partitioning (distributive law)</p>	<p>Show the links with arrays to illustrate the PV partitioning</p>  <p>4 rows of 10 4 rows of 3</p> <p>Move onto base ten to move towards a more compact method.</p>  <p>4 rows of 13</p> <p>Move on to place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows</p>	<p>Children can represent their work with place value counters in a way that they understand.</p> <p>They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown below.</p> 	$4 \times 10 = 40$ $4 \times 3 = 12$ $40 + 12 = 52$								
<p>2 digit x 1 digit using PV counters (no regrouping)</p>	<p>23 x 3</p> <table border="1" data-bbox="472 1007 842 1318"> <thead> <tr> <th>tens</th> <th>ones</th> </tr> </thead> <tbody> <tr> <td>10 10</td> <td>1 1 1</td> </tr> <tr> <td>10 10</td> <td>1 1 1</td> </tr> <tr> <td>10 10</td> <td>1 1 1</td> </tr> </tbody> </table> <p>Chn can see array in the ones and the tens. There is a visual link to repeated addition.</p>	tens	ones	10 10	1 1 1	10 10	1 1 1	10 10	1 1 1	<p>Children practice, drawing their representations.</p> 	$\begin{array}{r} 23 \\ \times 3 \\ \hline 69 \end{array}$
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10 10	1 1 1										
10 10	1 1 1										
10 10	1 1 1										

# Y4 MULTIPLICATION X

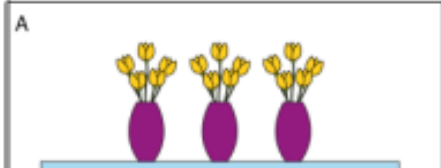

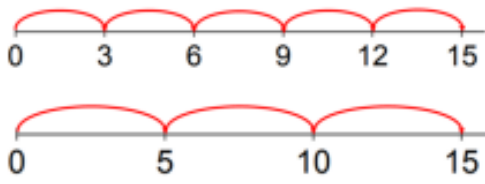


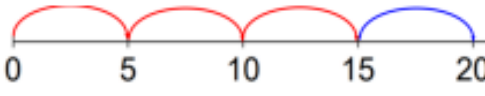
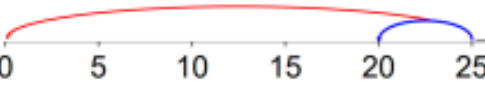
Objective & Strategy	Concrete	Pictorial	Abstract
<p>Understand the 3 times table</p>	<p>Count in three using objects and representations of multiples of 3.</p> 		<p>There are 12 wheels.</p> $4 \times 3 = 12$ $3 \times 4 = 12$
<p>Understand the 6 times table</p>	<p>We can double our 3 times table to find our 6 times table.</p> 		$12 \times 3 = 36$ $6 \times 6 = 36$
<p>Understand the 9 times table</p>	<p>Count in nines using objects and representations of multiples of 9. Make links 9 being three groups of three.</p> 		<p>There are 36 apples.</p> $4 \times 9 = 36$ $9 \times 4 = 36$



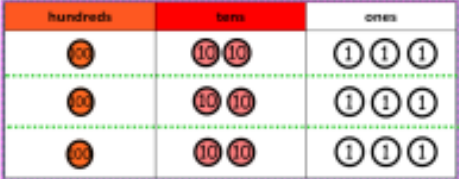
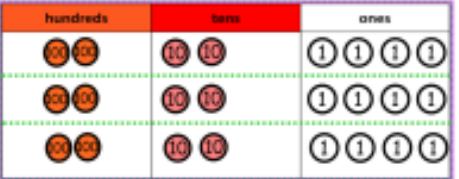

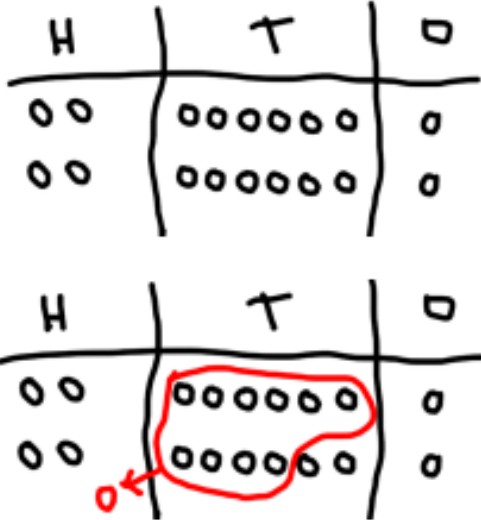
Objective & Strategy	Concrete	Pictorial	Abstract
<p>Understand the 7 times table</p>	<p>Children use representations which show groups of 7 including real life contexts.</p> 	<p>Linear models show jumps of 7.</p> 	<p>There are 14 players.</p> $2 \times 7 = 14$ $7 \times 2 = 14$

# Y4 MULTIPLICATION X

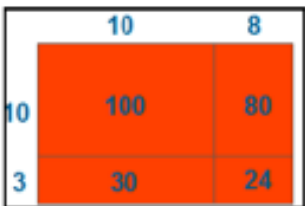

# Y4 MULTIPLICATION X

Objective & Strategy	Concrete	Pictorial	Abstract
<p>Understanding the commutative law.</p>	<p>A</p>  <ul style="list-style-type: none"> <li>• 'Three groups of five are equal to fifteen.'</li> <li>• 'Five, three times is equal to fifteen.'</li> </ul> <p>B</p>  <ul style="list-style-type: none"> <li>• 'Five groups of three are equal to fifteen.'</li> </ul> <p>"Three groups of five is equal to five groups of three."</p>		$3 \times 5 = 15$ $5 \times 3 = 15$ $5 \times 3 = 3 \times 5 = 15$ $15 \div 3 = 5$ $15 \div 5 = 3$
<p>Understanding the distributive law</p>	 	 	$4 \times 5 = 3 \times 5 + 5 = 20$ $4 \times 5 = 5 \times 5 - 5 = 20$

# Y4 MULTIPLICATION X

Objective & Strategy	Concrete	Pictorial	Abstract
<p>Multiply 3 digit numbers by 1 digit. (no exchange)</p>	<p>Use place value counters to show how we are finding groups of a number. We are multiplying by 3 so we need 3 rows</p> <p><math>123 \times 3 = 369</math></p>  <p>300 + 60 + 9</p> <p>Add up each column, starting with the ones.</p>	<p>Children can represent their work with place value counters by drawing place value counters or Dienes.</p>	$\begin{array}{r} 231 \\ \times 3 \\ \hline 693 \end{array}$ <p>3 x 1 ones is three ones</p> <p>3 x 3 tens is nine tens</p> <p>3 x 2 hundreds is six hundreds</p>
<p>Multiply 3 digit numbers by 1 digit. (with exchange)</p>	<p><math>224 \times 3</math></p>  <p>600 + 70 + 2</p> <p>Regroup ten ones to make a new ten.</p>  <p>600 + 70 + 2</p> <p>We can take 10 ones to make a new ten.</p> <p>600 + 70 + 2</p> <p>+672</p>	<p><math>261 \times 2</math></p>  <p>500 + 20 + 2</p> <p>+522</p>	$\begin{array}{r} 241 \\ \times 4 \\ \hline 964 \\ 1 \end{array}$ <p>4 times 1 ones is 4 ones</p> <p>4 times 4 tens is 16 tens. I put 6 tens down and carry ten tens which is now a hundred.</p> <p>4 times 2 hundreds is 8 hundreds. I add the hundred I have carried to make 9 hundreds.</p>

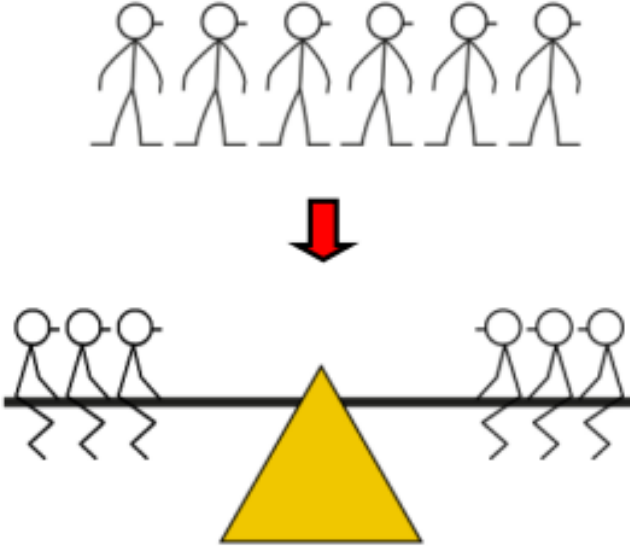
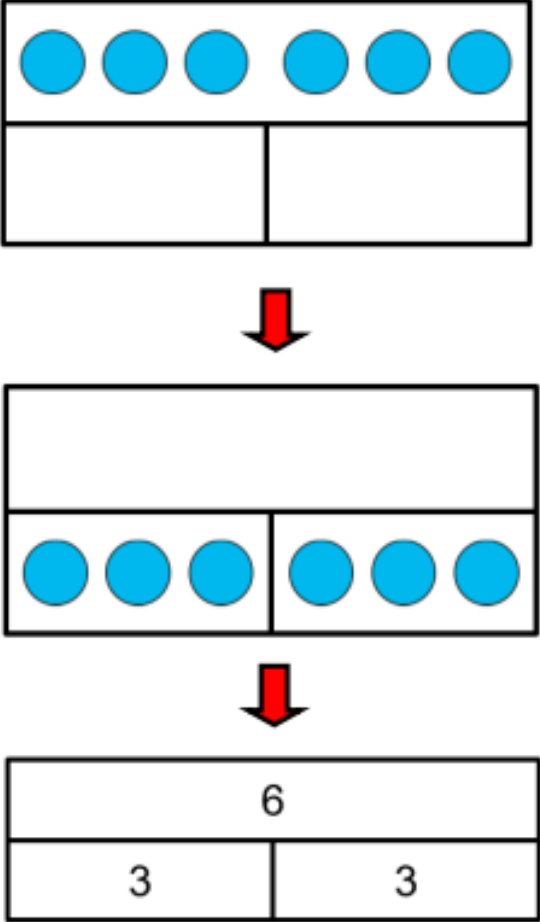
# Y5 MULTIPLICATION X

Objective & Strategy	Concrete	Pictorial	Abstract																														
<p>Multiply 3 and 4 digits x 1 digit.</p>	<p>Children may continue to be supported by place value counters at the stage of multiplication. This initially done where there is no regrouping.</p> <p>3024 x 3</p> <table border="1" data-bbox="387 470 873 638"> <thead> <tr> <th>thousands</th> <th>hundreds</th> <th>tens</th> <th>ones</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> <td></td> </tr> </tbody> </table> <p>900 + 0 + 60 +</p>	thousands	hundreds	tens	ones																	<p>Children may continue to draw their understanding using place value grids.</p>	$\begin{array}{r} 3024 \\ \times \quad 3 \\ \hline 9072 \\ \phantom{0}1 \end{array}$										
thousands	hundreds	tens	ones																														
<p>Multiply up to 4 digits by 2 digits</p>	<p>Manipulatives may still be used with the corresponding long multiplication modelled alongside.</p> <p>Begin with teen number x teen number.</p> <p>Progress to any 2–4 digit number x 2 digit.</p>	 <p>10      8</p> <p>100    80</p> <p>30     24</p>	 <p>18 x 3 on the first row</p> <p>(8 x 3 = 24, carrying the 2 for 20, then 1 x 3)</p> <p>18 x 10 on the 2nd row. Show multiplying by 10 by putting zero in units first</p> <table border="1" data-bbox="1478 1165 1668 1460"> <thead> <tr> <th></th> <th>100s</th> <th>10s</th> <th>1s</th> <th></th> </tr> </thead> <tbody> <tr> <td></td> <td></td> <td>3</td> <td>1</td> <td></td> </tr> <tr> <td>x</td> <td></td> <td>2</td> <td>4</td> <td></td> </tr> <tr> <td></td> <td>1</td> <td>2</td> <td>4</td> <td>31 x 4</td> </tr> <tr> <td></td> <td>6</td> <td>2</td> <td>0</td> <td>31 x 20</td> </tr> <tr> <td></td> <td>7</td> <td>4</td> <td>4</td> <td></td> </tr> </tbody> </table>		100s	10s	1s				3	1		x		2	4			1	2	4	31 x 4		6	2	0	31 x 20		7	4	4	
	100s	10s	1s																														
		3	1																														
x		2	4																														
	1	2	4	31 x 4																													
	6	2	0	31 x 20																													
	7	4	4																														



# Y6 MULTIPLICATION X


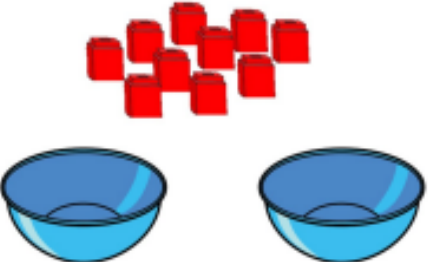
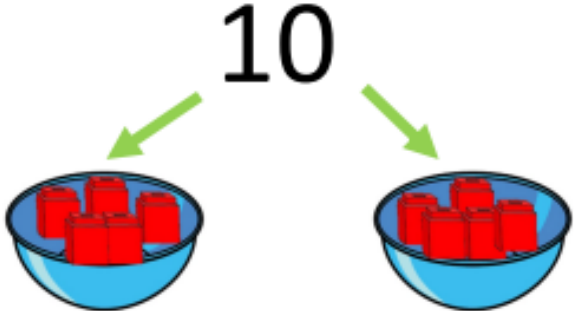
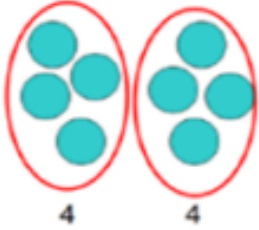
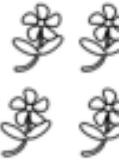
Objective & Strategy	Concrete	Pictorial	Abstract
Multiply decimals up to 2 decimal places by a single digit			$\begin{array}{r} 2.38 \\ \times \quad 3 \\ \hline 714 \\ \color{red}{12} \end{array}$ <p>First we lay out the calculation</p> <p>Next, we write the decimal point in the answer (product).</p> <p>Finally, we carry out the multiplication.</p> <p><i>3 x 8 hundredths is 24 hundredths</i></p> <p><i>3 x 3 tenths is 9 tenths, add 2 tenths we carried is 11 tenths</i></p> <p><i>3 x 3 ones is 6 ones, add 1 one we carried is 7 ones</i></p>
Multiply up to 4 digit numbers by 2 digits.			$\begin{array}{r} \phantom{312} \cancel{4} \\ \phantom{312} 3 \phantom{1} 2 \\ \times \phantom{312} 28 \\ \hline 2496 \\ 6240 \\ \hline 8736 \\ \phantom{8736} 1 \end{array}$

Objective & Strategy	Concrete	Pictorial
<p>Find half of numbers to 20.</p>	<p>Real life and practical contexts are used to find half of numbers up to 20.</p> 	<p>Children use manipulatives to represent real life problems.</p>  <p>half of 6 = 3 double 3 = 6</p>

**Y1**

**DIVISION**


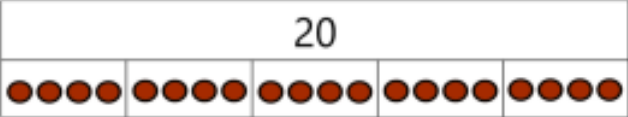
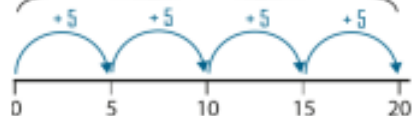
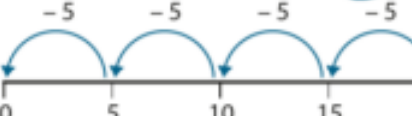
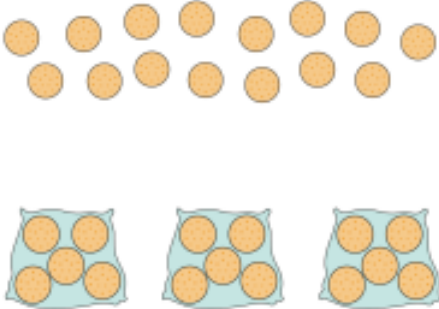
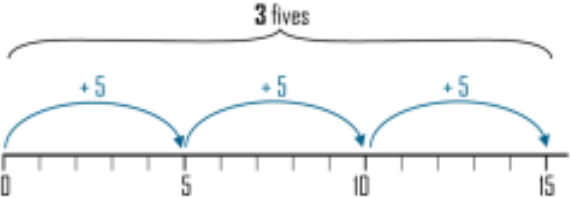
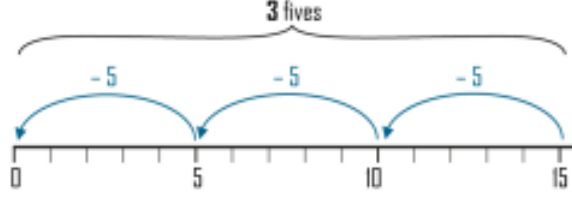
**÷**

Objective & Strategy	Concrete	Pictorial
<p>Understand division as sharing into equal groups</p> <p>Use Gordon ITPs for modelling</p>	<p>Children solve real life problems using real objects.</p>  <p>There are eight sweets. Daisy and Will share these equally. How many do they get each?</p> <p>I have 10 cubes, can you share them equally in 2 groups?</p>  <p>There are 2 equal groups. Each group has 5.</p> 	<p>Children use pictures or shapes to share quantities.</p>  <p>8 shared between 2 is 4</p>  <p>10 shared between 2 is 5</p>

# Y1

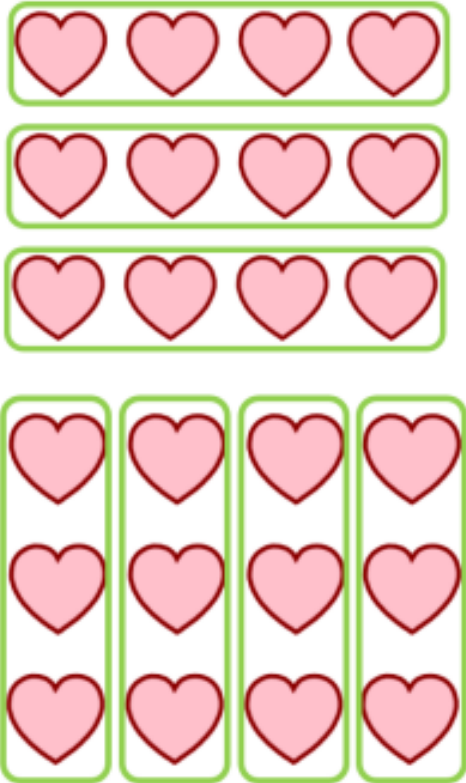
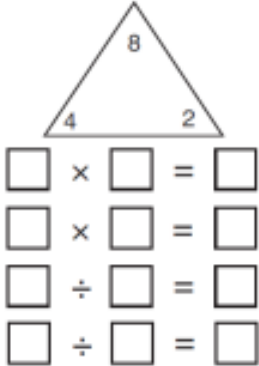
# DIVISION

# ÷

Objective & Strategy	Concrete	Pictorial	Abstract
Division as sharing (partitive)	<p>There are 20 conkers shared equally between 5 children.</p>  <p>Each child gets 4 conkers.</p>	<p>Children use pictures or shapes to share quantities. They may use bar modelling to show and support understanding.</p>  <p>Number lines are used to show skip counting (counting forwards)</p>  <p>and repeated subtraction (counting backwards).</p> 	$20 \div 5 = 4$
Division as grouping (quotitive)	<p>Use cubes, counters or real objects to aid understanding.</p> <p>There are 15 biscuits, there are 5 in each bag. How many bags?</p> 	 <p>3 fives</p> $5 + 5 + 5 = 15$ $15 \div 5 = 3$  <p>3 fives</p> $15 - 5 - 5 - 5 = 0$ $15 \div 5 = 3$	<p>15 divided into groups of 5 is 3</p> $15 \div 5 = 3$


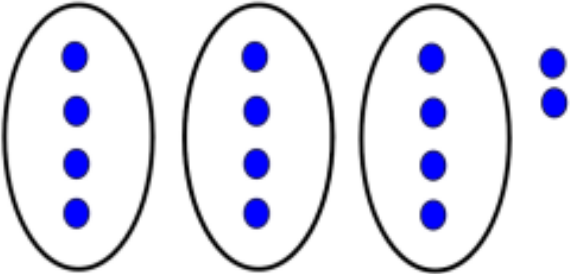


# Y2 DIVISION ÷



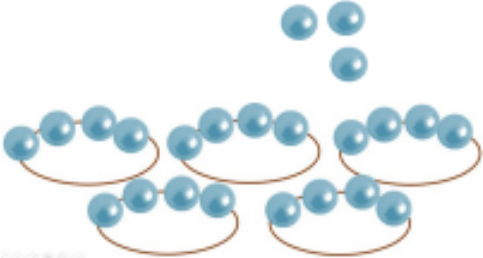

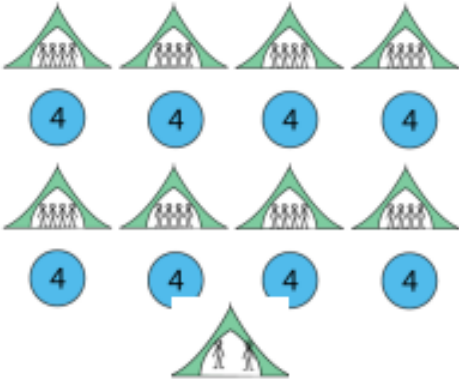
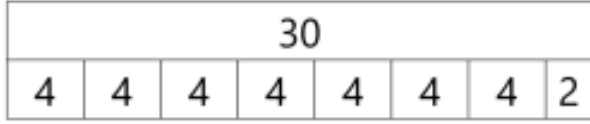
Objective & Strategy	Concrete	Pictorial	Abstract
Understanding the Inverse			<p> <math>3 \times 4 = 12</math>  <math>12 \div 4 = 3</math> </p> <p> <math>4 \times 3 = 12</math>  <math>12 \div 3 = 4</math> </p> <p> <math>2 \times 4 = 8</math>      <math>4 \times 2 = 8</math>  <math>8 \div 2 = 4</math>      <math>8 \div 4 = 2</math>  <math>8 = 2 \times 4</math>      <math>8 = 4 \times 2</math>  <math>2 = 8 \div 4</math>      <math>4 = 8 \div 2</math> </p> <p>Show all 8 related fact family sentences.</p>

# Y2

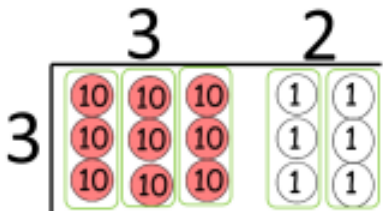
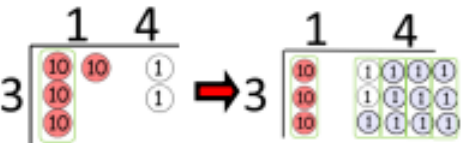
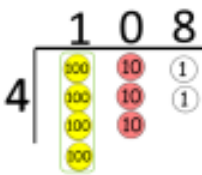
# DIVISION ÷

Objective & Strategy	Concrete	Pictorial	Abstract										
Division with remainders. (partitive)	<p>I divide 14 cakes between 3 plates. How are the cakes shared?</p> 	<p>Draw dots and group them to divide an amount and clearly show a remainder.</p> 	<p>Complete written divisions and show the remainder using r.</p> $14 \div 3 = 4 \text{ r } 2$ <p style="text-align: center;"> <span style="margin-right: 20px;">↓</span> <span style="margin-right: 20px;">↓</span> <span style="margin-right: 20px;">↓</span> <span>↓</span>            dividend    divisor    quotient    remainder         </p>										
Division with remainders. (quotitive)	<p>13 eggs are put into boxes. Each box holds 3 eggs. How are the eggs boxed?</p> 	<p>Children may draw representations to show their understanding.</p>  <p>Use bar models to show division with remainders.</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td colspan="5" style="text-align: center;">13</td> </tr> <tr> <td style="text-align: center;">3</td> <td style="text-align: center;">3</td> <td style="text-align: center;">3</td> <td style="text-align: center;">3</td> <td style="text-align: center;">1</td> </tr> </table>	13					3	3	3	3	1	$13 \div 3 = 4 \text{ r } 1$
13													
3	3	3	3	1									

# Y3 DIVISION ÷

Objective & Strategy	Concrete	Pictorial	Abstract
Interpreting division with remainders.	<p>Bracelets are made using 4 beads. There are 23 beads. How many bracelets can be made? How many beads left over?</p> 	<p>Bar model representations may be used.</p> 	$23 \div 4 = 5 \text{ r } 3$
Interpreting division with remainders.	<p>4 scouts can fit in each tent. How many tents needed for 30 scouts?</p> 		$30 \div 4 = 7 \text{ r } 2$ <p>8 tents are needed.</p> <p>Discuss with pupils the need to round up in this context.</p>

# Y4 DIVISION ÷

Objective & Strategy	Concrete	Pictorial	Abstract
<p>Divide 2 and 3 digit numbers by 1 digit.</p> <p>Short Division</p>	<p><math>96 \div 3</math></p> <p>Use place value counters to make groups of the divisor, starting with the largest value digit.</p>  <p>There are 3 groups of 3 tens.</p> <p>There are 2 groups of 3 ones.</p> <p><math>42 \div 3</math></p>  <p>There is 1 group of 3 tens. There is a ten left over. We exchange this for 10 ones. 12 ones divided by 3 is 4</p> <p><math>432 \div 4</math></p>  <p>There is 1 group of 4 hundreds. There are no groups of 4 tens and three tens left over.</p> <p>There are 8 groups of 4 ones.</p>	<p>Students use drawn diagrams with dots or circles to show their understanding.</p>	<p>Begin with divisions that divide equally with no remainder.</p> $3 \overline{) 124}$ <p>Move onto divisions with a remainder. Return to concrete if necessary.</p> $4 \overline{) 138} r3$

**Y4**

**DIVISION**

**÷**



Objective & Strategy	Concrete	Pictorial	Abstract
Divide decimals by a single digit, using x and ÷ by 10 or 100			<p>Pupils use understanding of x and ÷ 10 to make connections.</p> $\begin{array}{r} 6.3 \div 9 = 0.7 \\ \times 10 \downarrow \\ 63 \div 9 = 7 \end{array} \quad \div 10$
Short division of decimals			<p>Children build on work from year 4, now with decimals</p> $\begin{array}{r} 0.41 \\ 6 \overline{) 2.46} \end{array}$

**Y5**  
**÷**  
**DIVISION**  
**÷**

**Division of 2 digits by 2 digits**Using  $\times$  &  $\div$  by 10, 100 etc and relating this to a short division method.

$$\begin{array}{r} 60 \div 30 = \boxed{2} \\ \div 10 \downarrow \quad \downarrow 10 \div \\ 6 \div 3 = 2 \end{array}$$

$$\begin{array}{r} 0 \quad 2 \\ 30 \overline{) 6 \quad 60} \end{array}$$



### Long Division—2 digits divided by 2 digits

Y6  
DIVISION ÷

H T O

$$30 \overline{) 85}$$

30 does not go into 8.  
So, combine the 8  
tens with the 5 ones.

H T O

$$30 \overline{) 85} \begin{array}{r} 2 \\ 60 \end{array}$$

30 goes into 85 twice,  
which is 60.

H T O

$$30 \overline{) 85} \begin{array}{r} 2 \\ \underline{60} \\ 25 \end{array}$$

Subtract the 60 from  
the 85 and this leaves  
25.

H T O

$$30 \overline{) 85} \begin{array}{r} 2 \text{ r } 25 \\ \underline{60} \\ 25 \end{array}$$

85 divided by 30 is 2  
with a remainder of  
25

## Moving to Long division of 2 digits by 2 digits

### Making a 'useful' list

H T O  
 $31 \overline{) 434}$

	X 31
1	31
2	
3	
4	
5	
6	
7	
8	
9	
10	

	X 31
1	31
2	62
3	
4	
5	
6	
7	
8	
9	
10	

Double 1x  
to find 2 x

x10

	X 31
1	31
2	62
3	
4	
5	
6	
7	
8	
9	
10	310

Double 1x  
to find 2 x

	X 31
1	31
2	62
3	
4	
5	155
6	
7	
8	
9	
10	310

Double 1x  
to find 2 x

Halve 10x  
to find 5 x

x10

	X 31
1	31
2	62
3	
4	124
5	155
6	
7	
8	
9	
10	310

Double 1x  
to find 2 x

Double 2x  
to find 4 x

Halve 10x  
to find 5 x

x10

	X 31
1	31
2	62
3	93
4	124
5	155
6	186
7	217
8	248
9	279
10	310

Double 1x  
to find 2 x

Double 2x  
to find 4 x

Halve 10x  
to find 5 x

# Y6

# DIVISION ÷





## Long Division—3 digits divided by 2 digits

$$\begin{array}{r} \text{H} \quad \text{T} \quad \text{O} \\ 31 \overline{) 4 \quad 3 \quad 4} \end{array}$$

$$\begin{array}{r} \text{H} \quad \text{T} \quad \text{O} \\ 0 \\ 31 \overline{) 4 \quad 3 \quad 4} \end{array}$$

31 does not go into 4 (hundreds).

$$\begin{array}{r} \text{H} \quad \text{T} \quad \text{O} \\ 0 \quad 1 \\ 31 \overline{) 4 \quad 3 \quad 4} \\ \underline{3 \quad 1} \end{array}$$

We combine the 4 hundreds with the tens to give 43 tens. 31 goes into 43 once which is 31, we record this underneath.

$$\begin{array}{r} \text{H} \quad \text{T} \quad \text{O} \\ 0 \quad 1 \\ 31 \overline{) 4 \quad 3 \quad 4} \\ \underline{3 \quad 1} \\ 1 \quad 2 \end{array}$$

Subtract to find the remainder. 31 from 43 leaves 12.

$$\begin{array}{r} \text{H} \quad \text{T} \quad \text{O} \\ 0 \quad 1 \\ 31 \overline{) 4 \quad 3 \quad 4} \\ \underline{3 \quad 1} \\ 1 \quad 2 \quad 4 \end{array}$$

We combine 12 with the next digit to give 124.

$$\begin{array}{r} \text{H} \quad \text{T} \quad \text{O} \\ 0 \quad 1 \\ 31 \overline{) 4 \quad 3 \quad 4} \\ \underline{3 \quad 1} \\ 1 \quad 2 \quad 4 \\ \underline{1 \quad 2 \quad 4} \end{array}$$

31 goes into 124 four times, which is 124.

$$\begin{array}{r} \text{H} \quad \text{T} \quad \text{O} \\ 0 \quad 1 \quad 4 \\ 31 \overline{) 4 \quad 3 \quad 4} \\ \underline{3 \quad 1} \\ 1 \quad 2 \quad 4 \\ \underline{1 \quad 2 \quad 4} \\ 0 \end{array}$$

We subtract to show there is no remainder

Y6  
DIVISION ÷

## Long Division—progressing to 4 or more digits

$$\begin{array}{r} \text{TH} \quad \text{H} \quad \text{T} \quad \text{O} \\ 23 \overline{) 4 \quad 9 \quad 4 \quad 5} \end{array}$$



$$\begin{array}{r} \text{TH} \quad \text{H} \quad \text{T} \quad \text{O} \\ \quad \quad 2 \\ 23 \overline{) 4 \quad 9 \quad 4 \quad 5} \\ \underline{4 \quad 6} \phantom{0} \\ \quad \quad 3 \phantom{0} \end{array}$$



$$\begin{array}{r} \text{TH} \quad \text{H} \quad \text{T} \quad \text{O} \\ \quad \quad 2 \quad 1 \\ 23 \overline{) 4 \quad 9 \quad 4 \quad 5} \\ \underline{4 \quad 6} \phantom{0} \\ \quad \quad 3 \quad 4 \\ \quad \quad \underline{2 \quad 3} \\ \quad \quad \quad 1 \quad 1 \end{array}$$

23 goes into 49 twice which is 46. We subtract this from 49 to give a remainder of 3.

We combine the 3 left over with the next digit to give 34. 23 goes into 34 once with 11 remaining.



$$\begin{array}{r} \text{TH} \quad \text{H} \quad \text{T} \quad \text{O} \\ \quad \quad 2 \quad 1 \quad 5 \\ 23 \overline{) 4 \quad 9 \quad 4 \quad 5} \\ \underline{4 \quad 6} \phantom{0} \\ \quad \quad 3 \quad 4 \\ \quad \quad \underline{2 \quad 3} \\ \quad \quad \quad 1 \quad 1 \quad 5 \\ \quad \quad \quad \underline{1 \quad 1 \quad 5} \\ \quad \quad \quad \quad \quad 0 \end{array}$$

We combine the 11 with the next digit to make 115. 23 goes into 115 5 times with no remainder.



### Long Division—procedural summary (remainder in the tens)

Y6  
DIVISION ÷

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
$\begin{array}{r} \text{t o} \\ 2 \overline{)58} \end{array}$ <p>Two goes into 5 two times, or 5 tens ÷ 2 = 2 whole tens -- but there is a remainder!</p>	$\begin{array}{r} \text{t o} \\ 2 \overline{)58} \\ -4 \phantom{0} \\ \hline 1 \phantom{0} \end{array}$ <p>To find it, multiply <math>2 \times 2 = 4</math>, write that 4 under the five, and subtract to find the remainder of 1 ten.</p>	$\begin{array}{r} \text{t o} \\ 29 \\ 2 \overline{)58} \\ -4 \phantom{0} \\ \hline 18 \end{array}$ <p>Next, drop down the 8 of the ones next to the leftover 1 ten. You combine the remainder ten with 8 ones, and get 18.</p>

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
$\begin{array}{r} \text{t o} \\ 29 \\ 2 \overline{)58} \\ -4 \phantom{0} \\ \hline 18 \end{array}$ <p>Divide 2 into 18. Place 9 into the quotient.</p>	$\begin{array}{r} \text{t o} \\ 29 \\ 2 \overline{)58} \\ -4 \phantom{0} \\ \hline 18 \\ -18 \\ \hline 0 \end{array}$ <p>Multiply <math>9 \times 2 = 18</math>, write that 18 under the 18, and subtract.</p>	$\begin{array}{r} \text{t o} \\ 29 \\ 2 \overline{)58} \\ -4 \phantom{0} \\ \hline 18 \\ -18 \\ \hline 0 \end{array}$ <p>The division is over since there are no more digits in the dividend. The quotient is 29.</p>



### Long Division—procedural summary (remainder in any of the digits)

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
$\begin{array}{r} \text{h t o} \\ 1 \\ 2 \overline{) 278} \end{array}$ <p>Two goes into 2 one time, or 2 hundreds + 2 = 1 hundred.</p>	$\begin{array}{r} \text{h t o} \\ 1 \\ 2 \overline{) 278} \\ -2 \\ \hline 0 \end{array}$ <p>Multiply <math>1 \times 2 = 2</math>, write that 2 under the two, and subtract to find the remainder of zero.</p>	$\begin{array}{r} \text{h t o} \\ 18 \\ 2 \overline{) 278} \\ -2 \downarrow \\ \hline 07 \end{array}$ <p>Next, drop down the 7 of the tens next to the zero.</p>
Divide.	Multiply & subtract.	Drop down the next digit.
$\begin{array}{r} \text{h t o} \\ 13 \\ 2 \overline{) 278} \\ -2 \\ \hline 07 \end{array}$ <p>Divide 2 into 7. Place 3 into the quotient.</p>	$\begin{array}{r} \text{h t o} \\ 13 \\ 2 \overline{) 278} \\ -2 \\ \hline 07 \\ -6 \\ \hline 1 \end{array}$ <p>Multiply <math>3 \times 2 = 6</math>, write that 6 under the 7, and subtract to find the remainder of 1 ten.</p>	$\begin{array}{r} \text{h t o} \\ 13 \\ 2 \overline{) 278} \\ -2 \\ \hline 07 \\ -6 \\ \hline 18 \end{array}$ <p>Next, drop down the 8 of the ones next to the 1 leftover ten.</p>
1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
$\begin{array}{r} \text{h t o} \\ 139 \\ 2 \overline{) 278} \\ -2 \\ \hline 07 \\ -6 \\ \hline 18 \end{array}$ <p>Divide 2 into 18. Place 9 into the quotient.</p>	$\begin{array}{r} \text{h t o} \\ 139 \\ 2 \overline{) 278} \\ -2 \\ \hline 07 \\ -6 \\ \hline 18 \\ -18 \\ \hline 0 \end{array}$ <p>Multiply <math>9 \times 2 = 18</math>, write that 18 under the 18, and subtract to find the remainder of zero.</p>	$\begin{array}{r} \text{h t o} \\ 139 \\ 2 \overline{) 278} \\ -2 \\ \hline 07 \\ -6 \\ \hline 18 \\ -18 \\ \hline 0 \end{array}$ <p>There are no more digits to drop down. The quotient is 139.</p>

Y6  
DIVISION ÷



<b>Divisibility rules in 'families' – 2, 4 and 8</b>	
<b>2</b>	A number is divisible by 2 if the ones digit is even.
<b>4</b>	If halving a number gives an even value, then the number is divisible by 4. <i>and</i> For numbers with more than two digits: if the final two digits are divisible by 4 then the number is divisible by 4.
<b>8</b>	If halving a number twice gives an even value, the number is divisible by 8.



<b>Divisibility rules in 'families' – 5 and 10</b>	
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<b>5</b>	A number is divisible by 5 if the ones digit is 5 or 0.
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<b>10</b>	A number is divisible by 10 if the ones digit is 0.
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<b>2</b>	A number is divisible by 2 if the ones digit is even.
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<b>Divisibility rules in numerical order</b>	
<b>2</b>	A number is divisible by 2 if the ones digit is even.
<b>3</b>	For a number to be divisible by 3, the sum of the digits of the number must be divisible by 3.
<b>4</b>	If halving a number gives an even value, then the number is divisible by 4. <i>and</i> For numbers with more than two digits: if the final two digits are divisible by 4 then the number is divisible by 4.
<b>5</b>	A number is divisible by 5 if the ones digit is 5 or 0.
<b>6</b>	For a number to be divisible by 6, the number must be divisible by <i>both 2 and 3</i> .
<b>8</b>	If halving a number twice gives an even value, the number is divisible by 8.
<b>9</b>	For a number to be divisible by 9, the sum of the digits of the number must be divisible by 9.
<b>10</b>	A number is divisible by 10 if the ones digit is 0.